



# NARSIMHA REDDY ENGINEERING COLLEGE

## UGC AUTONOMOUS INSTITUTION

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### UNIT-II

#### Continuous Distributions and Sampling

| S. No                             | Questions                                                                                                                                                                                                                                                                                                                                                                                                    | BT   | CO   | PO   |   |   |      |      |      |      |       |     |     |     |
|-----------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|------|------|---|---|------|------|------|------|-------|-----|-----|-----|
| Part – A (Short Answer Questions) |                                                                                                                                                                                                                                                                                                                                                                                                              |      |      |      |   |   |      |      |      |      |       |     |     |     |
| 1                                 | Define expectation of a random variable X                                                                                                                                                                                                                                                                                                                                                                    | L1   | CO2  | PO1  |   |   |      |      |      |      |       |     |     |     |
| 2                                 | Define variance of a random variable X for discrete and continuous cases.                                                                                                                                                                                                                                                                                                                                    | L1   | CO2  | PO1  |   |   |      |      |      |      |       |     |     |     |
| 3                                 | Let X be a random variable with density function<br>$f(x) = \begin{cases} \frac{x^3}{3}, & -1 < x < 2 \\ 0, & \text{else where} \end{cases}$<br>Find the expected value of g(x)=4x+3                                                                                                                                                                                                                         | L3   | CO2  | PO2  |   |   |      |      |      |      |       |     |     |     |
| 4                                 | Let the random variable X represent the number of defective parts for a machine when 3 parts are sampled from a production line and tested. The following is the probability distribution of X.<br><table border="1"><tr><td>X</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>F(x)</td><td>0.51</td><td>0.38</td><td>0.10</td><td>0.01</td></tr></table><br>Calculate E(X) and E(X <sup>2</sup> ). | X    | 0    | 1    | 2 | 3 | F(x) | 0.51 | 0.38 | 0.10 | 0.01  | L3  | CO2 | PO2 |
| X                                 | 0                                                                                                                                                                                                                                                                                                                                                                                                            | 1    | 2    | 3    |   |   |      |      |      |      |       |     |     |     |
| F(x)                              | 0.51                                                                                                                                                                                                                                                                                                                                                                                                         | 0.38 | 0.10 | 0.01 |   |   |      |      |      |      |       |     |     |     |
| 5                                 | 20% of item produced from a factory are defective. Find the probability that in a sample of 5 chosen at random P(1<x<4).                                                                                                                                                                                                                                                                                     | L3   | CO2  | PO2  |   |   |      |      |      |      |       |     |     |     |
| 6                                 | If the probability of a defective bolt is 0.2 find the mean and variances of the number of successes.                                                                                                                                                                                                                                                                                                        | L3   | CO2  | PO2  |   |   |      |      |      |      |       |     |     |     |
| 7                                 | Define geometric distribution.                                                                                                                                                                                                                                                                                                                                                                               | L1   | CO2  | PO1  |   |   |      |      |      |      |       |     |     |     |
| 8                                 | If a random variable has a Poisson distribution such that P(1) =P(2), find mean of the distribution.                                                                                                                                                                                                                                                                                                         | L3   | CO2  | PO2  |   |   |      |      |      |      |       |     |     |     |
| 9                                 | Using Poisson distribution, find the probability that the ace of spades will be drawn from a pack of well shuffled cards at least once in 104 consecutive trials.                                                                                                                                                                                                                                            | L3   | CO2  | PO2  |   |   |      |      |      |      |       |     |     |     |
| 10                                | In 256 set of 12 tosses of a coin, in how many cases one can expect 8 heads and 4 tails.                                                                                                                                                                                                                                                                                                                     | L3   | CO2  | PO2  |   |   |      |      |      |      |       |     |     |     |
| Part – B (Long Answer Questions)  |                                                                                                                                                                                                                                                                                                                                                                                                              |      |      |      |   |   |      |      |      |      |       |     |     |     |
| 11                                | Seven coins are tossed and the number of heads are noted. The experiment is repeated 128 times and the following distribution is obtained. Fit a Binomial Distribution to the following data assuming the coin is unbiased<br><table border="1"><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr></table>                                                  | x    | 0    | 1    | 2 | 3 | 4    | 5    | 6    | 7    | L3,L5 | CO2 | PO3 |     |
| x                                 | 0                                                                                                                                                                                                                                                                                                                                                                                                            | 1    | 2    | 3    | 4 | 5 | 6    | 7    |      |      |       |     |     |     |

|      |     |                                                                                                                                                                                                                                                                                                   |          |     |     |    |    |      |     |     |     |     |    |     |
|------|-----|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|-----|-----|----|----|------|-----|-----|-----|-----|----|-----|
|      |     | <table><tr><td>f</td><td>7</td><td>6</td><td>19</td><td>35</td><td>30</td><td>23</td><td>7</td><td>1</td></tr></table>                                                                                                                                                                            | f        | 7   | 6   | 19 | 35 | 30   | 23  | 7   | 1   |     |    |     |
| f    | 7   | 6                                                                                                                                                                                                                                                                                                 | 19       | 35  | 30  | 23 | 7  | 1    |     |     |     |     |    |     |
| 12   | a)  | Using recurrence formula find the probabilities when $X=0,1,2,3,4$ and 5, if the mean of Poisson distribution is 3.                                                                                                                                                                               | L3,L5    | CO2 | PO3 |    |    |      |     |     |     |     |    |     |
|      | b)  | If the probability that an individual suffers a bad reaction from a certain injection is 0.001, determine the probability that out of 2000 individuals<br><br>i. Exactly 3<br>ii. More than 2 individuals<br>iii. None<br>iv. More than one individual suffers bad reaction                       | L3       | CO2 | PO2 |    |    |      |     |     |     |     |    |     |
| 13   | a)  | Derive mean and variance of Geometric Distribution                                                                                                                                                                                                                                                | L1       | CO2 | PO1 |    |    |      |     |     |     |     |    |     |
|      | b)  | The weekly demand for a drinking-water product, in thousands of liters, from a local chain of efficiency stores is a continuous random variable X having the probability density. Find mean and variance.<br><br>$f(x) = \begin{cases} 2(x-1); & 1 < x < 2 \\ 0; & \text{else where} \end{cases}$ | L3       | CO2 | PO2 |    |    |      |     |     |     |     |    |     |
| 14   |     | Out of 800 families with 5 children each, how many would you expect to have<br><br>a. 3boys<br>b. 5girls<br>c. At least one boy<br>d. Mean<br>e. Variance                                                                                                                                         | L3,L4,L5 | CO2 | PO3 |    |    |      |     |     |     |     |    |     |
| 15   | a)  | Derive mean and variance of Poisson distribution                                                                                                                                                                                                                                                  | L1       | CO2 | PO1 |    |    |      |     |     |     |     |    |     |
|      | b)  | A die is tossed until 6 appears. Find the probability that it must be cast more than 5 times.                                                                                                                                                                                                     | L2       | CO2 | PO2 |    |    |      |     |     |     |     |    |     |
| 16   | a)  | If a Poisson Distribution is such that $\frac{3}{2}P(X=1) = P(X=3)$ . Find<br><br>i. $P(X \geq 1)$<br>ii. $P(X \leq 3)$                                                                                                                                                                           | L2       | CO2 | PO2 |    |    |      |     |     |     |     |    |     |
|      | b)  | Calculate the variance of $g(X)=2X+3$ , where X is a random variable with the following probability distribution<br><br><table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>F(x)</td><td>1/4</td><td>1/8</td><td>1/2</td><td>1/8</td></tr></table>                          | x        | 0   | 1   | 2  | 3  | F(x) | 1/4 | 1/8 | 1/2 | 1/8 | L3 | CO2 |
| x    | 0   | 1                                                                                                                                                                                                                                                                                                 | 2        | 3   |     |    |    |      |     |     |     |     |    |     |
| F(x) | 1/4 | 1/8                                                                                                                                                                                                                                                                                               | 1/2      | 1/8 |     |    |    |      |     |     |     |     |    |     |